

# Water Targeting Models for Simultaneous Flowsheet Optimization

- ESI meeting -

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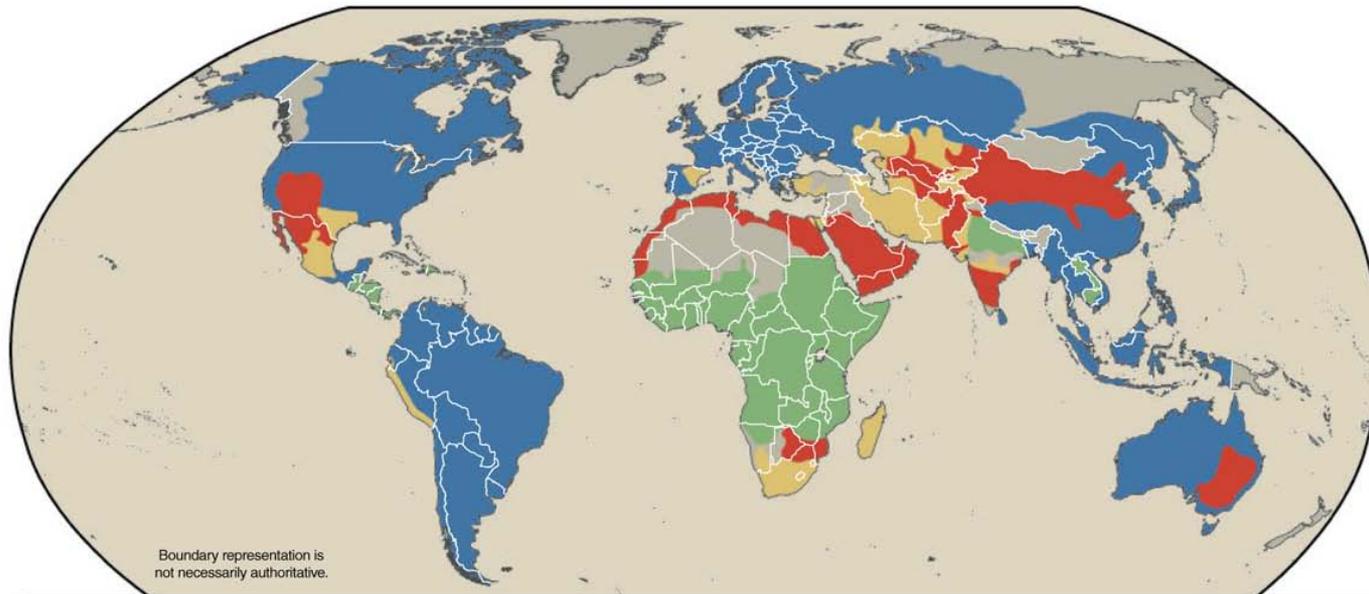
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# Water and energy are important resources in the process industries

“Water is the fastest growing market at the moment, with a size of \$500 billion globally.”

“If nothing is done, there will be a 40 percent gap between supply and demand by 2030.”

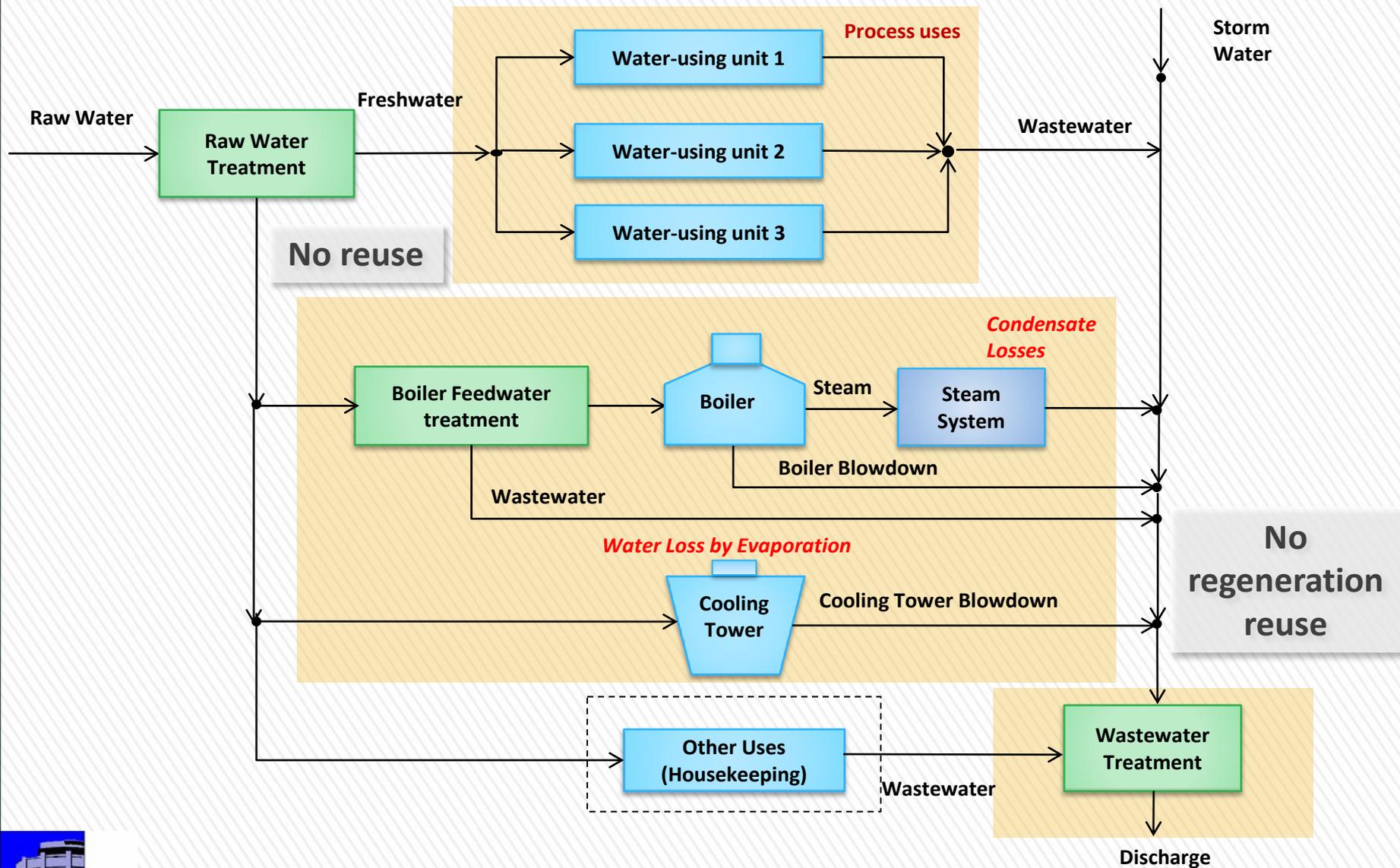
## Projected Global Water Scarcity, 2025



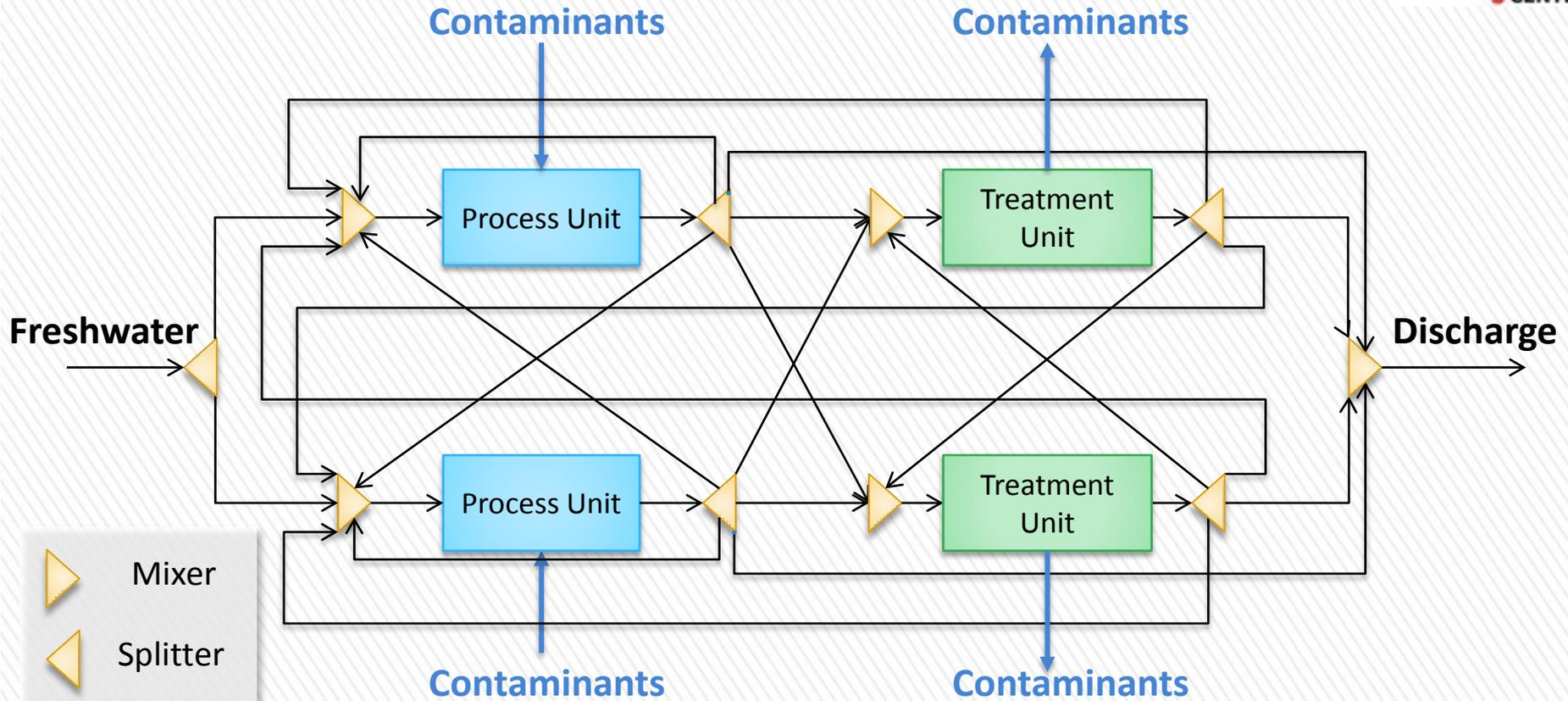
- Physical water scarcity:** More than 75% of river flows are allocated to agriculture, industries, or domestic purposes. This definition of scarcity — relating water availability to water demand — implies that dry areas are not necessarily water-scarce.
- Approaching physical water scarcity:** More than 60% of river flows are allocated. These basins will experience physical water scarcity in the near future.
- Economic water scarcity:** Water resources are abundant relative to water use, with less than 25% of water from rivers withdrawn for human purposes, but malnutrition exists.
- Little or no water scarcity:** Abundant water resources relative to use. Less than 25% of water from rivers is withdrawn for human purposes.
- Not estimated**

Source: International Water Management Institute.

# Conventional water network



# Superstructure based water network design



- » Integrated water network with reuse, recycle, and regeneration schemes
- » superstructure is formulated using a **nonconvex NLP** model

# Freshwater targeting formulation

**Goal: determine minimum freshwater consumption**

$$\min Z = F_{fw}$$

$$\text{s.t. } F^k = \sum_{i \in m_{in}} F^i \quad \forall m \in MU, k \in m_{out}$$

**Mixer mass  
balances**

$$F^k C_j^{k,\max} \geq \sum_{i \in m_{in}} (F^i C_j^{i,\max} + F_{fw}^i C_{fw}^i) \quad \forall j, \quad \forall m \in MU, k \in m_{out}$$

$$F^k = \sum_{i \in s_{out}} F^i \quad \forall s \in SU, k \in s_{in}$$

**Splitters mass  
balances**

$$C_j^k = C_j^i \quad \forall j, \quad \forall s \in SU, \quad \forall i \in s_{out}, k \in s_{in}$$

$$F^k = P_{in}^p \quad \forall p \in PU, k \in p_{out}$$

**Process  
unit mass  
balances**

$$F^i = P_{out}^p \quad \forall p \in PU, i \in p_{in}$$

$$F^i C_j^i + L_j^p = F^k C_j^k \quad \forall j, \forall p \in PU, i \in p_{in}, k \in p_{out}$$

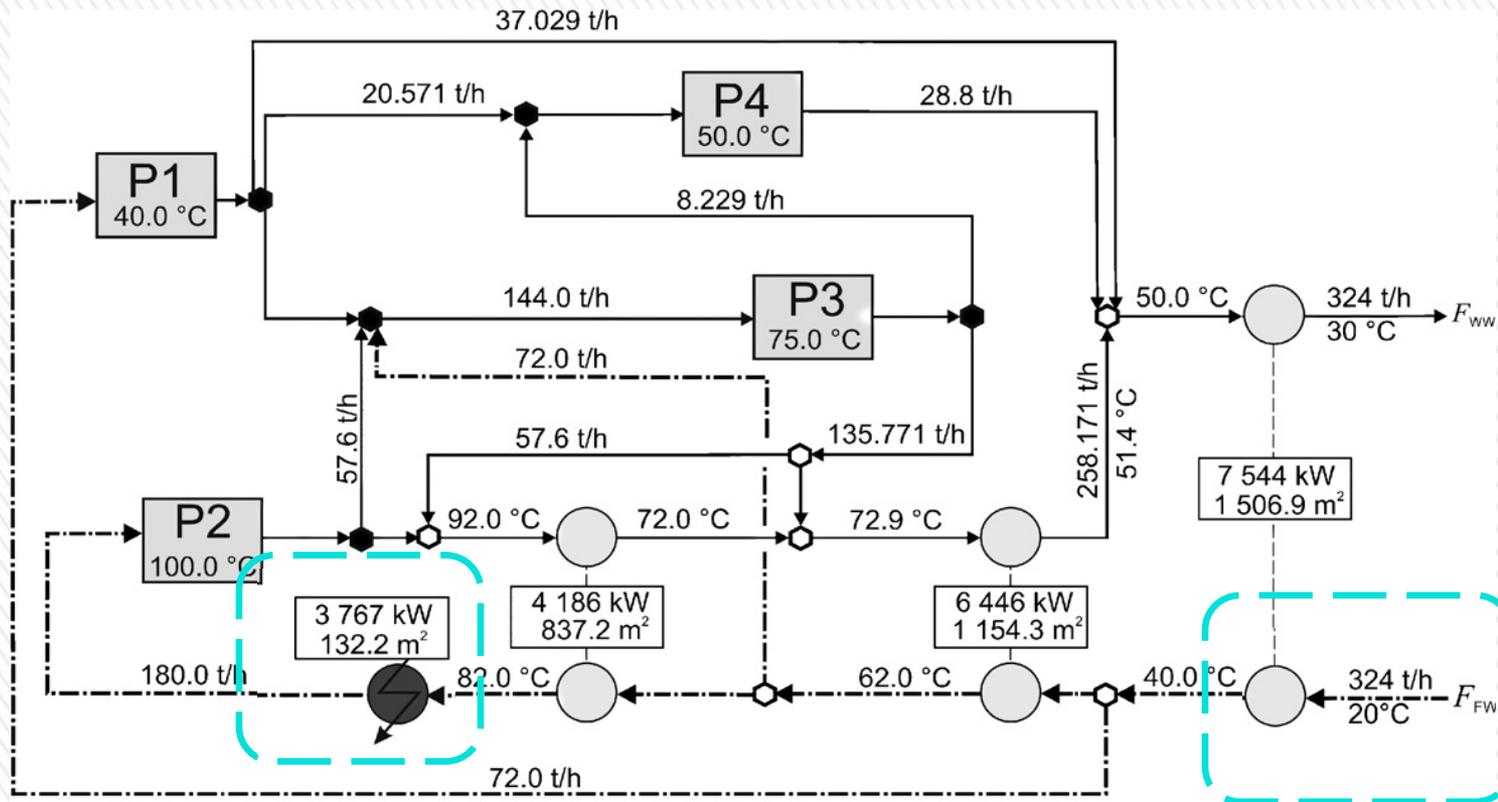
**(LP)**

**This formulation provides target for a network consists of a set of water-using process units using linear constraints**

Assumption: for some contaminant  $j$  that reaches its concentration upper bound at a given unit, it also reaches the upper bound at all other process units from which reuse streams have non-zero flowrate

# Heat-integrated WN reported in the literature

Use heat and water network formulation (**MINLP model**) to obtain network structure

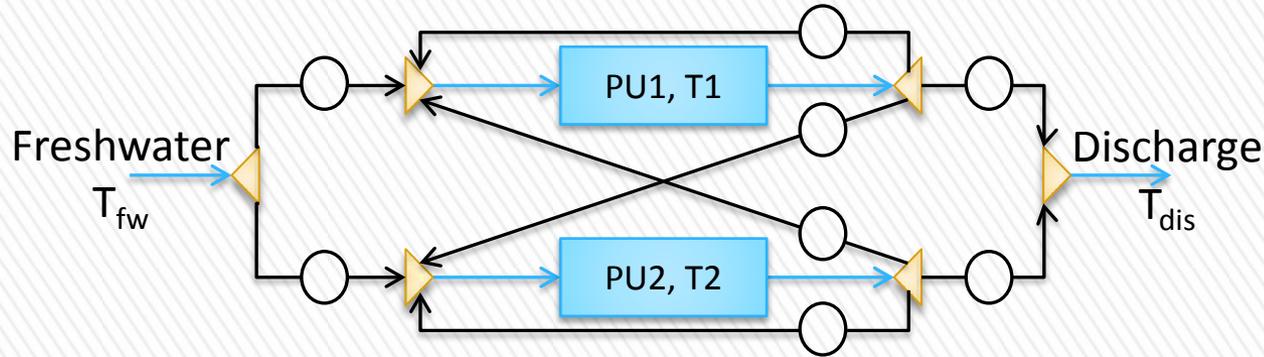


**LEGEND**

- > Fresh water stream
- > Polluted/waste water stream
- Mixing/splitting points determined in HEN superstructure
- Mixing/splitting points determined in WN superstructure

749 continuous variables  
115 binary variables

# Extension: heat-integrated water network



All black streams can participate in heat integration

## Objective fcn

$$\min. \phi = c_H Q_H + c_C Q_C + c_{fw} F_{fw}$$

## Water targeting (LP)

$$F^k = \sum_{i \in m_{in}} F^i \quad \forall m \in MU, k \in m_{out}$$

$$F^k C_j^{k,max} \geq \sum_{i \in m_{in}} (F^i C_j^{i,max} + F_{fw} C_{fw})$$

$$\forall j, \quad \forall m \in MU, k \in m_{out}$$

$$F^k = \sum_{i \in s_{out}} F^i \quad \forall s \in SU, k \in s_{in}$$

$$C_j^k = C_j^i \quad \forall j, \quad \forall s \in SU, \quad \forall i \in s_{out}, k \in s_{in}$$

$$F^k = P_{in}^p \quad \forall p \in PU, k \in p_{out}$$

$$F^i = P_{out}^p \quad \forall p \in PU, i \in p_{in}$$

$$F^i C_j^i + L_j^p = F^k C_j^k$$

$$\forall j, \forall p \in PU, i \in p_{in}, k \in p_{out}$$

## Heat targeting (LP)

$$Q_H \geq \sum_{js \in C \cup s_{out}} f_{js} c_{js} [\max\{0, t_{js}^{out} - (T^p - \Delta T_m)\}]$$

$$- \max\{0, t_{js}^{in} - (T^p - \Delta T_m)\}]$$

$$- \sum_{is \in H \cup s_{out}} F_{is} C_{is} [\max\{0, T_{is}^{in} - T^p\}]$$

$$- \max\{0, T_{is}^{out} - T^p\}]$$

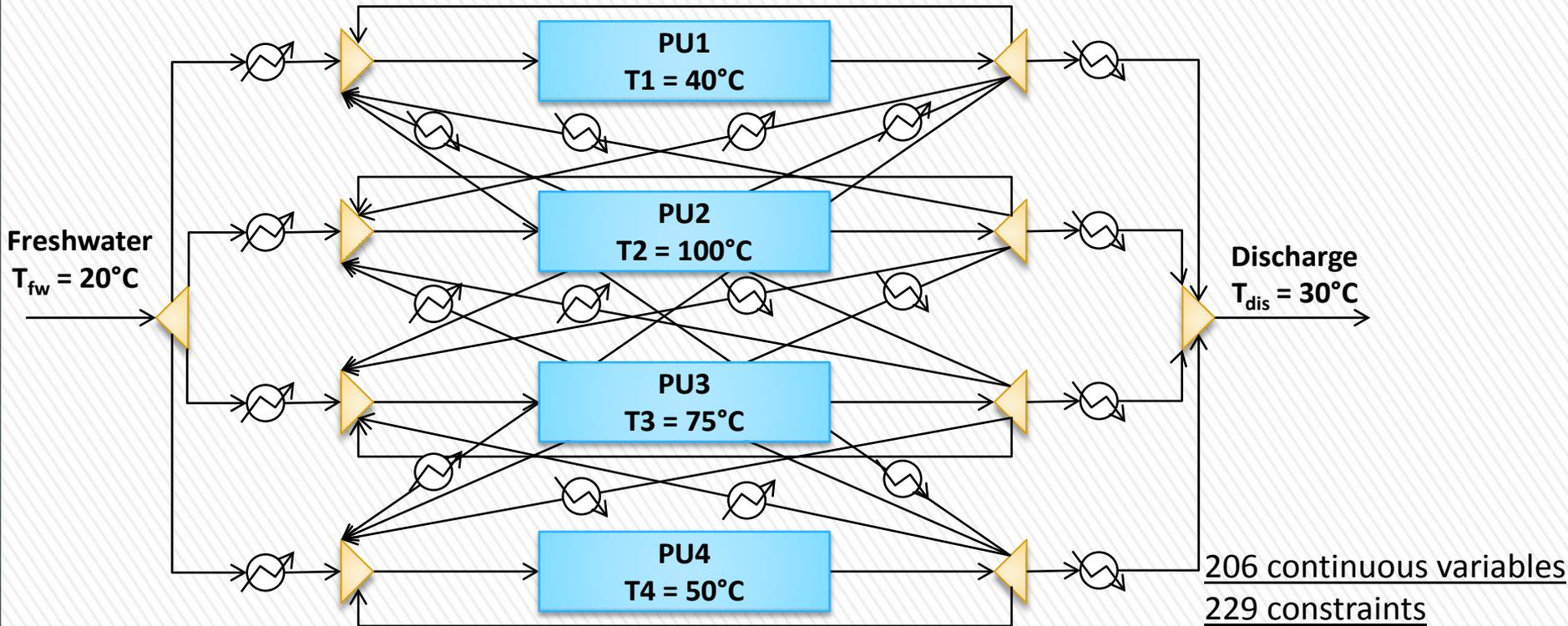
$$Q_C = Q_H + \sum_{is \in H \cup s_{out}} F_{is} C_{is} (T_{is}^{in} - T_{is}^{out})$$

$$- \sum_{js \in C \cup s_{out}} f_{js} c_{js} (t_{js}^{out} - t_{js}^{in})$$

$$T^p = T_{is}^{in} \quad \forall p = is \in H \cup s_{out} \quad \forall s \in SU$$

$$T^p = (t_{js}^{in} + \Delta T_m) \quad \forall p = js \in C \cup s_{out} \quad \forall s \in SU$$

# Revisit: heat-integrated water network utility targeting



## Parameter

$C_{HU}$ (\$/kW a)	260	$T_{HU}^{in}$ (°C)	126
$C_{CU}$ (\$/kW a)	150	$T_{HU}^{out}$ (°C)	126
$C_{FW}$ (\$/t)	2.5	$T_{CU}^{in}$ (°C)	15
HRAT (°C)	10	$T_{CU}^{out}$ (°C)	20

## Use heat and water targeting formulation:

Minimum heating utility: **3767 kW**

Minimum cooling utility : **No cooling utility required**

Minimum freshwater consumption: **324 ton/h**

Same result as network approach

# Simultaneous optimization strategy

$$\min. \phi = F(x, u, v) + \sum_{i \in HU} c_H^i Q_H^i + \sum_{j \in CU} c_C^j Q_C^j + c_{fw} F_{fw}$$

$$\text{s.t. } h(x, u, v) = 0$$

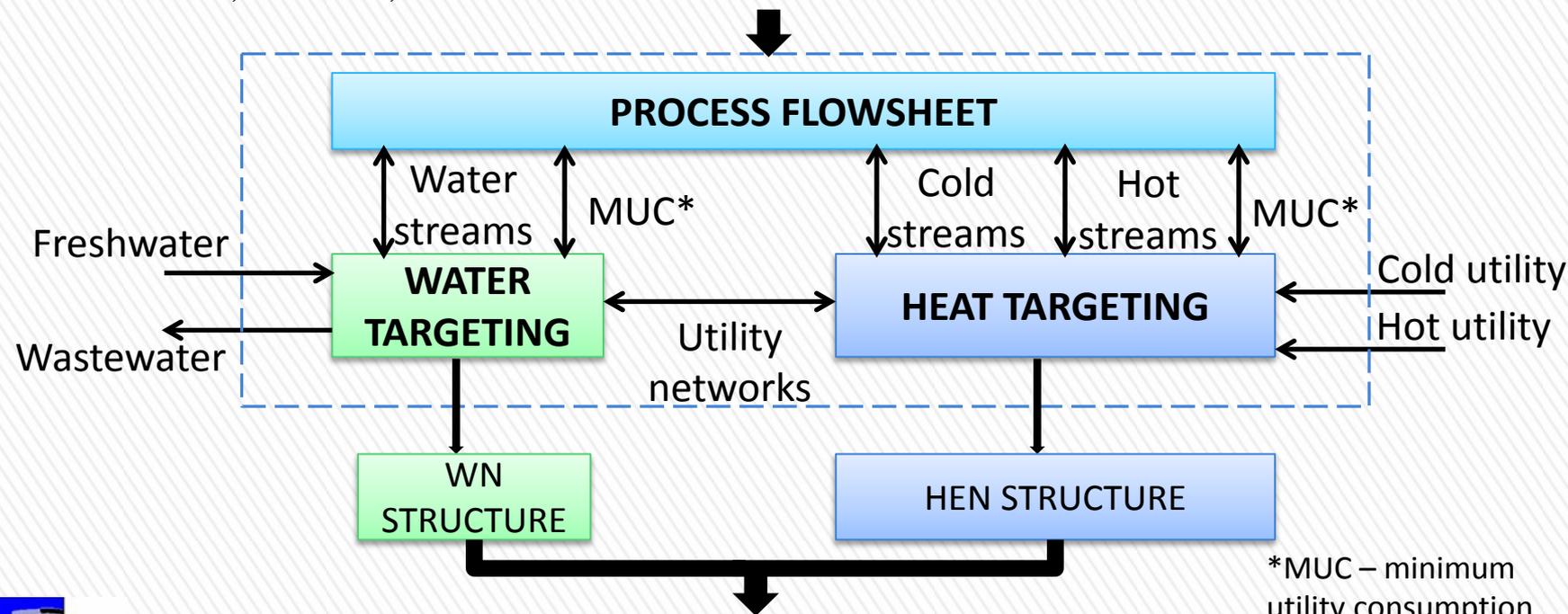
$$g^P(x, u, v) \leq 0$$

$$g^{HEN}(u, Q_H, Q_C) \leq 0$$

$$g^{WN}(v, F_{fw}) \leq 0$$

$$x \in X, \quad u \in U, \quad v \in V$$

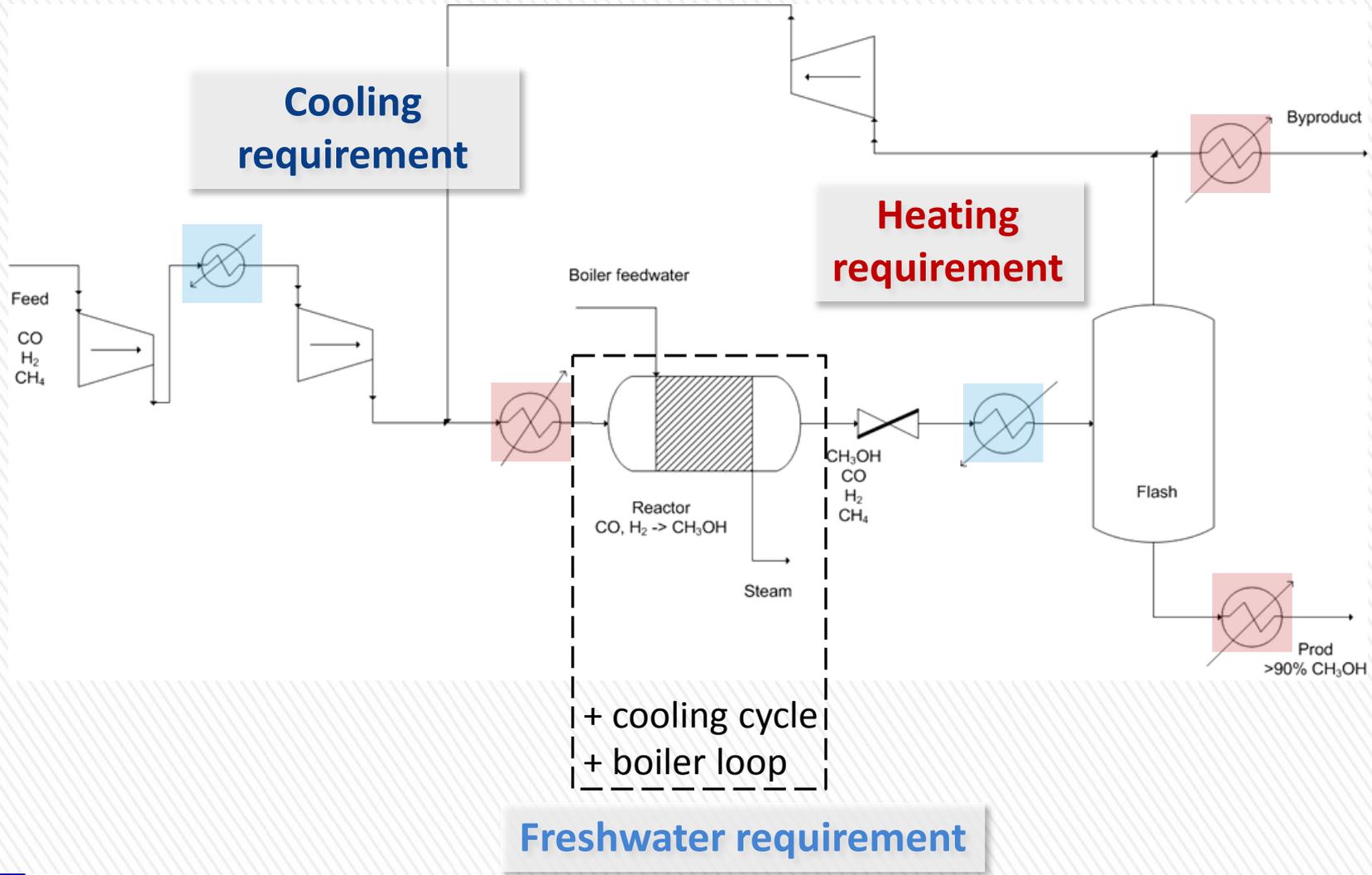
PROCESS STRUCTURE



\*MUC – minimum utility consumption

PROCESS FLOWSHEET WITH HEN AND WN

# Simultaneous optimization: methanol synthesis from syngas



# Sequential vs. simultaneous result comparison

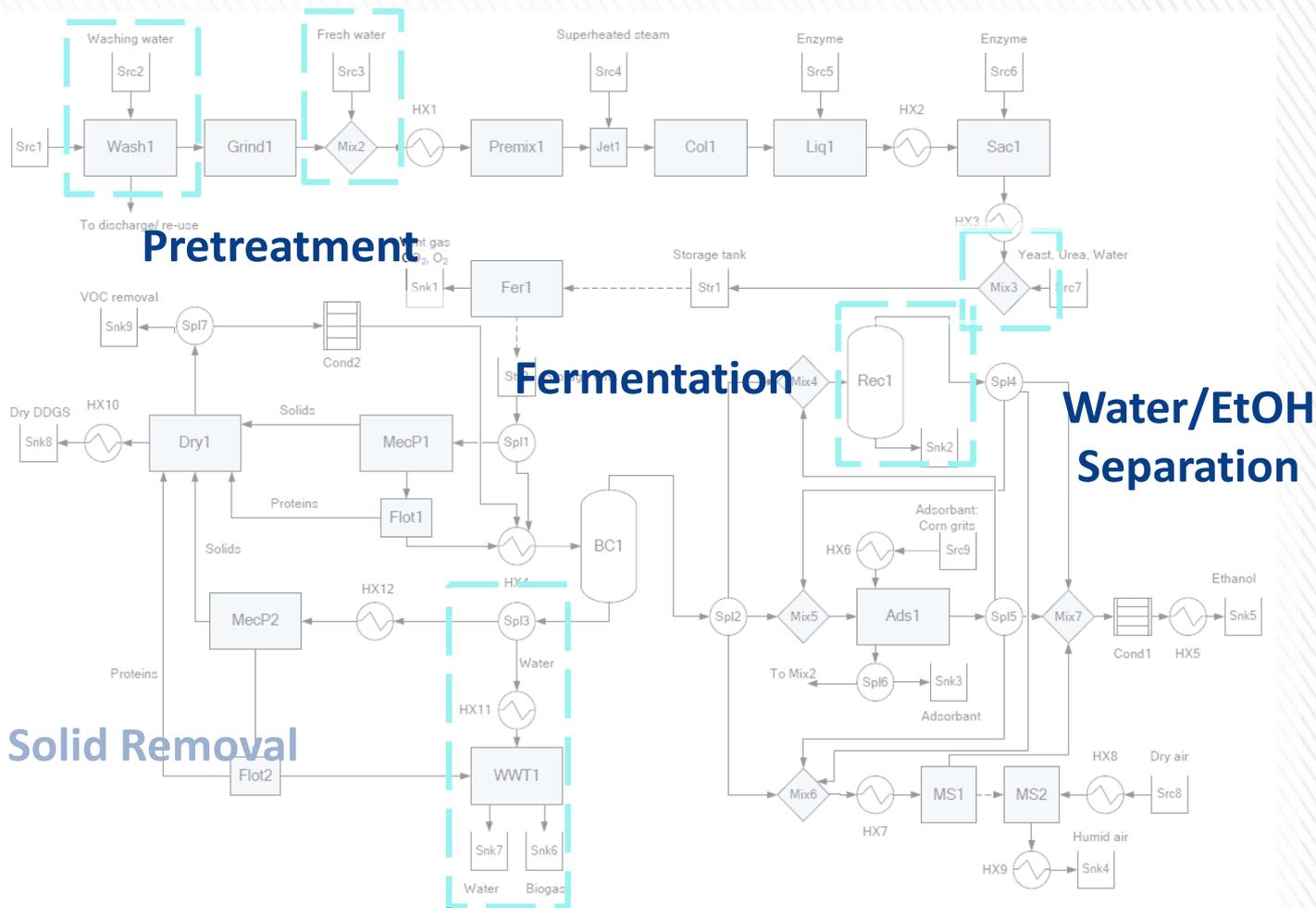
	SEQUENTIAL	SIMULTANEOUS
<b>Profit (1000 \$/yr)</b>	<b>62,695</b>	<b>73,416</b>
Investment cost (1000 \$)	1,891	1,174
Operating parameters		
electricity (KW)	6.59	1.84
freshwater (kg/s)	36.43	29.25
heating utility ( $10^9$ KJ/yr)	0.293	0
cooling utility ( $10^9$ KJ/yr)	67.3	72.7
Steam generated ( $10^9$ kJ/yr)	2448	1965
overall conversion	0.68	0.88
Material flowrate ( $10^6$ kmol/yr)		
feedstock	48.04	37.13
product	10.89	10.89

Solved with BARON 9

**17% improvement**

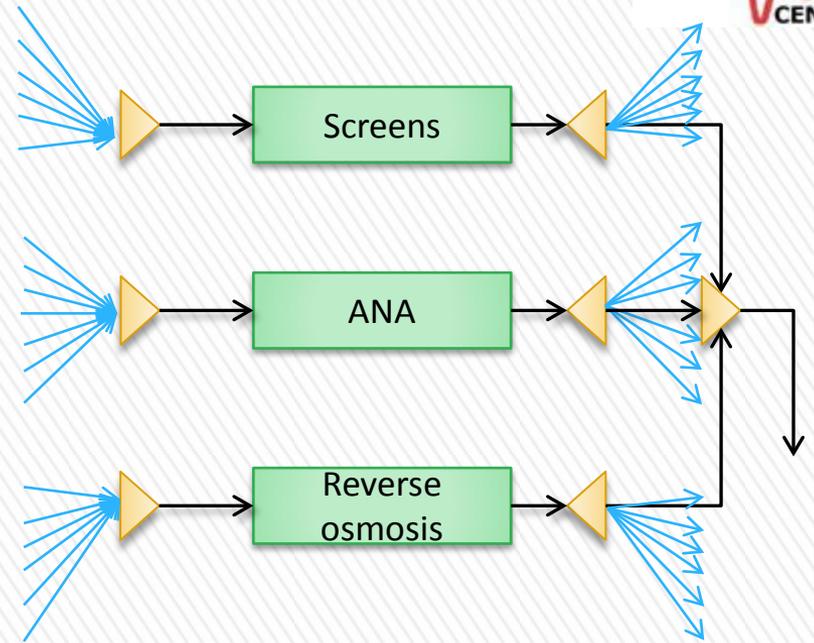
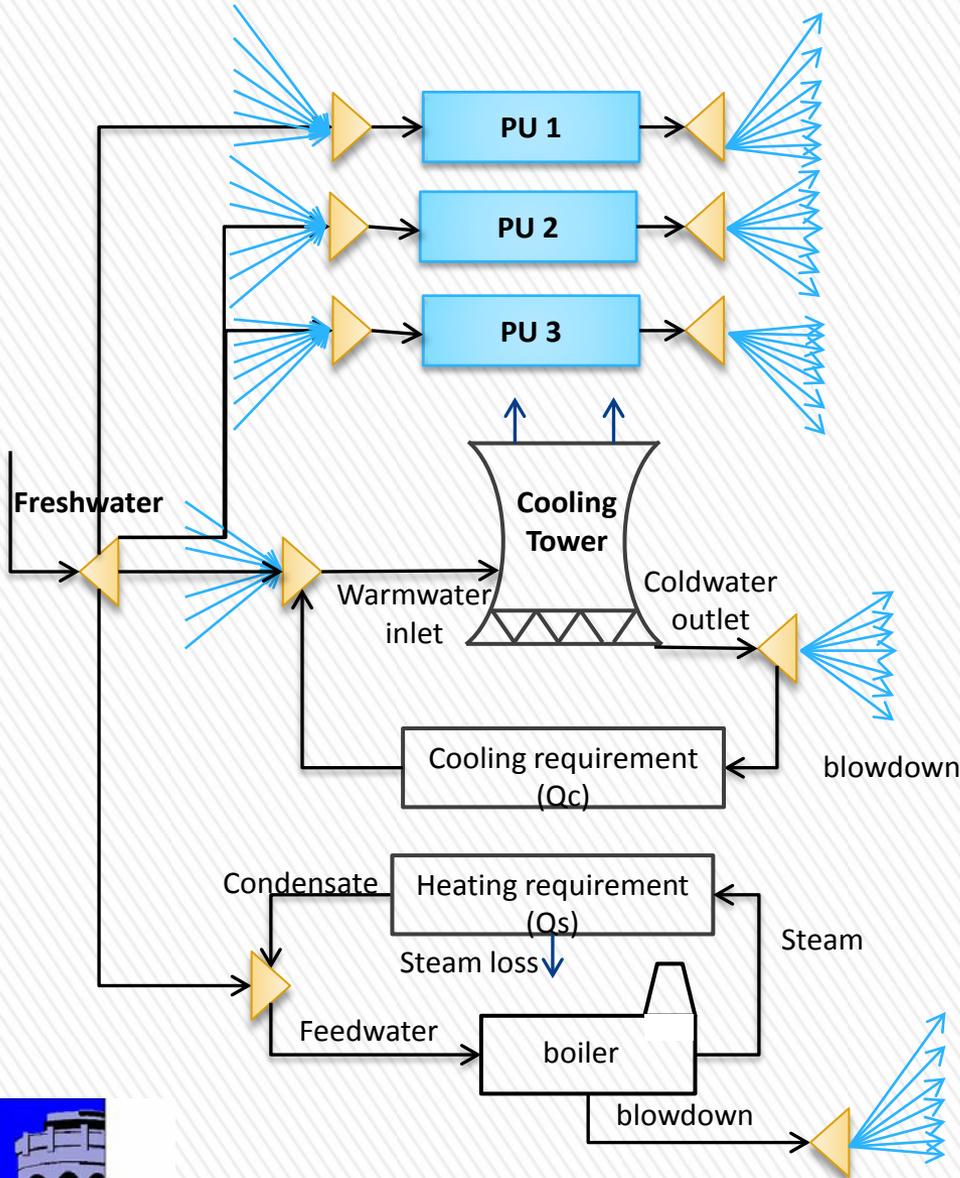
# Example 2: Bioethanol production

## Water Consumption and generation



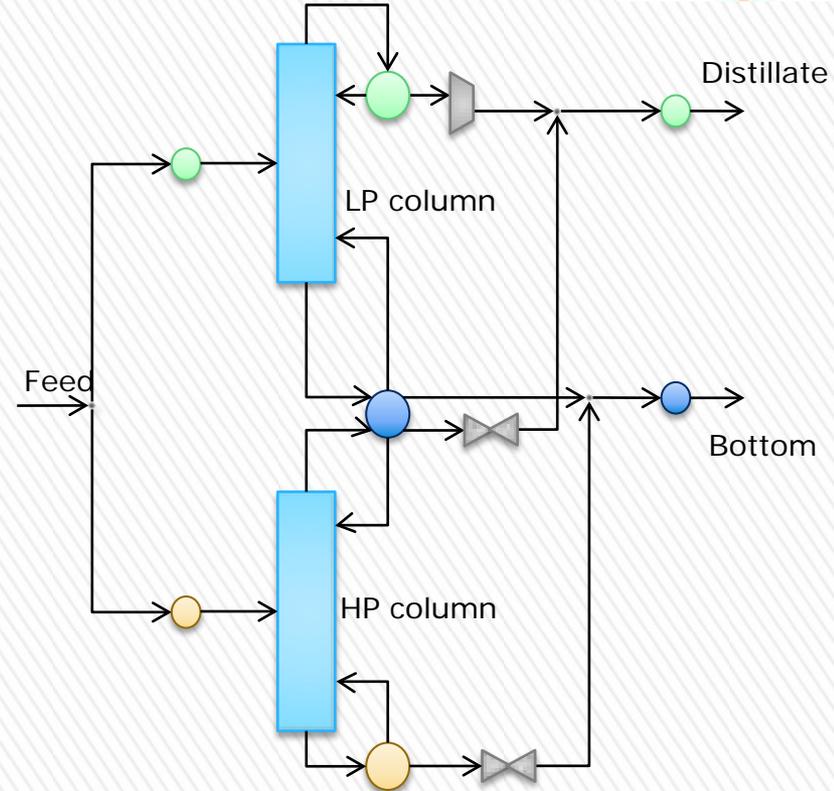
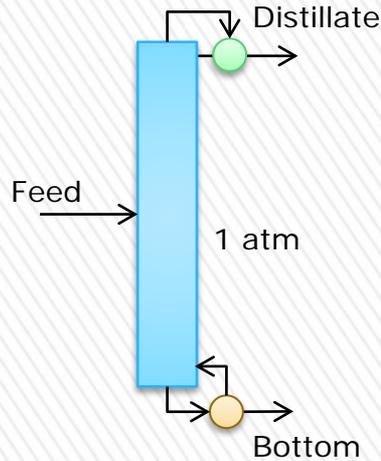
R. Karuppiyah, A. Peschel, I. E. Grossmann, M. Martin, W. son, and L. Zullo, "Energy optimization for the design of corn-based ethanol plants," *AIChE Journal*, vol. 54, no. 6, 2008, pp. 1499–1525.

# Water network superstructure



$C_j^{in,max}$ (ppm)	TSS	TDS	ORG
Boiler loop	2	100	10
Cooling cycle	10	500	10
1-B <sub>j</sub> <sup>t</sup>			
Screens	95%	0	0
Reverse osmosis	0	90%	0
Anaerobic tank	0	0	99%

# Multieffect columns



## Formulation

- > Dew point equation - condenser temperature
- > Bubble point equation - feed and reboiler temperature
- > Fenske equation - # of trays
- > Watson's equation – heat of vaporization
- > Mass balance
- > Energy balance

## Assumptions

- > Constant relative volatility
- > Ideal solution
- > Water is the only component contributing to heat of vaporization
- > Temperature change due to pumps is negligible

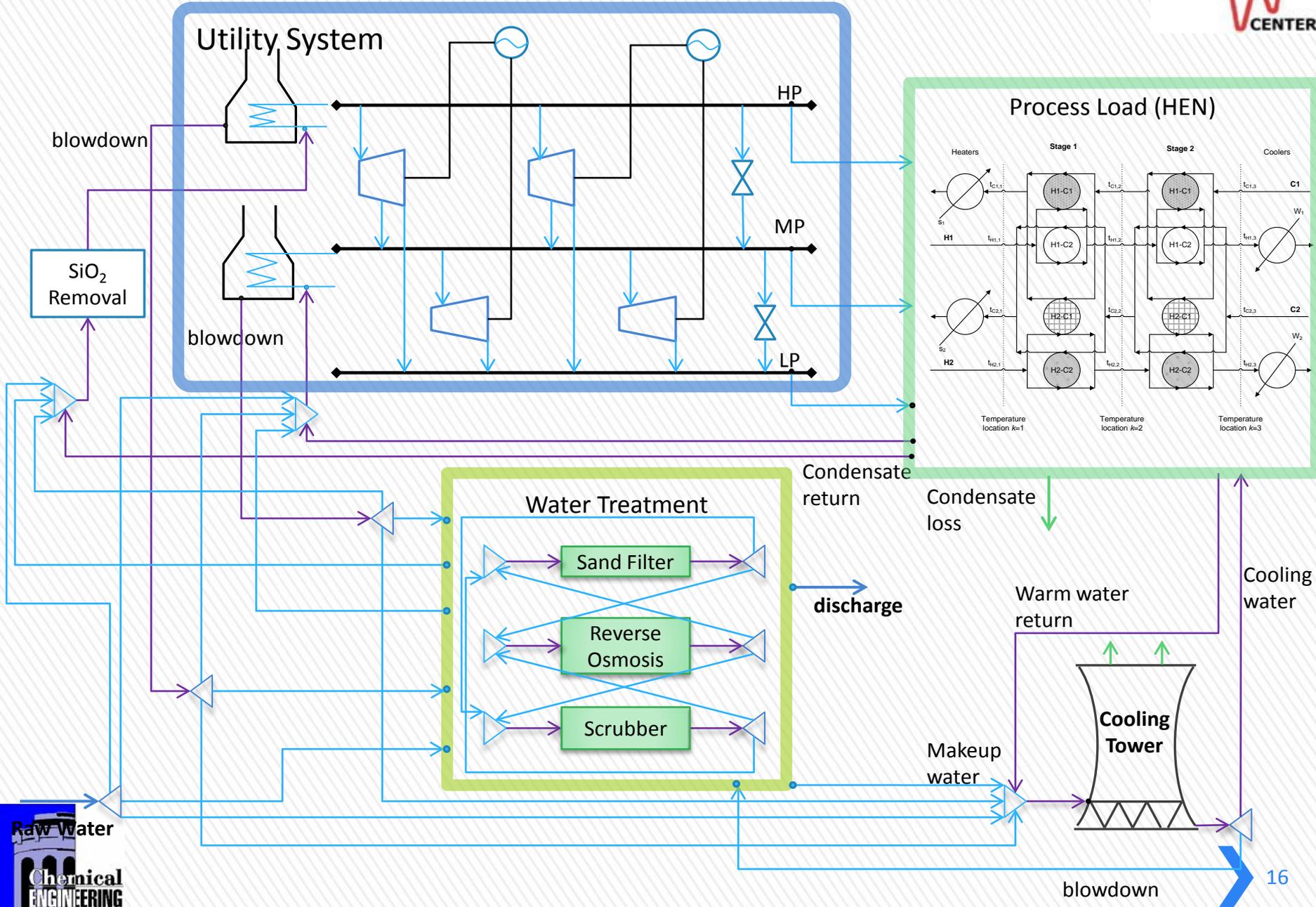
	No integration	Sequential single column	Sequential w/ multieffect	Simultaneous w/ Multieffect
Cost (MM\$/yr)	14.91	11.77	8.57	8.57
Cooling water use (kg/s)	2895.6	1998.3	1127.3	1124.8
Freshwater use (kg/s)	40.8	127.6	90.0	90.0
Steam use (kg/s)	35.1	28.3	21.2	21.3
CPU(s)	387	387	470	563
# eqns	2,232	2,232	3,213	5,221
# cont var	2,921	2,921	3,914	5,392

NLP solver: CONOPT 3  
 MINLP solver: BARON 9  
 GAMS 23.7

Even though the objective function did not improve using simultaneous method, we can see that the solution time did not increase drastically

**Reboiler duty reduced by ~36% by with multieffect column**

# Utility integration – power, water, & heat



# Problem statement

## Objective function

$$\phi = \underbrace{\sum_{st} c_b^{fix} Y_b^{st} + \sum_{st} c_b^{var} F_b^{st}}_{\text{Boiler cost}} + \underbrace{\sum_{st} \sum_d c_{tur}^{fix} Y_d^{st} + \sum_d c_{ext}^{fix} Y_d^{ext} + \sum_{st} \sum_d c_{tur}^{var} W_d^{st}}_{\text{Turbine cost}} + \underbrace{\sum_s c_s F_s}_{\text{Flowsheet stream cost}} + \underbrace{c_{fw} F_{fw}}_{\text{freshwater cost}}$$

Boiler cost

Turbine cost

Flowsheet stream cost  
freshwater cost

HEN	Utility system	WN
<ul style="list-style-type: none"> <li>• 2 hot streams/ 2 cold streams</li> <li>• Inlet and outlet temperature can vary within +/- 10 K</li> <li>• Heat capacity flowrate can vary within 20%</li> <li>• Two streams have assigned costs</li> <li>• Hot utility - HP, MP, and LP steam</li> <li>• Cold utility - cooling water</li> </ul>	<ul style="list-style-type: none"> <li>• Existence of boiler</li> <li>• Existence of turbine</li> <li>• Back pressure turbine</li> <li>• Extraction turbine (additional cost \$20,000)</li> <li>• Flowsheet power demand (7500kW)</li> <li>• 70% condensate return</li> </ul>	<ul style="list-style-type: none"> <li>• HP boiler has more stringent feedwater requirement</li> <li>• HP boiler/MP boiler have different blowdown rates</li> <li>• RO consumes electricity</li> <li>• Raw water needs treatment</li> <li>• TSS, TDS, GAS present in freshwater</li> <li>• Discharge limit imposed</li> </ul>
<p><b>Multiple hot utility targeting (Duran &amp; Grossmann)</b></p> <ul style="list-style-type: none"> <li>▪ Heating utilities targets</li> <li>▪ Cooling utility target</li> </ul>	<p><b>Utility system</b></p> <ul style="list-style-type: none"> <li>▪ Logical constraints</li> <li>▪ Demand constraints</li> <li>▪ Power balances</li> <li>▪ Mass balances</li> </ul>	<p><b>Water network</b></p> <ul style="list-style-type: none"> <li>▪ Mass balances</li> <li>▪ Power demand constraint</li> </ul>

	Sequential		Simultaneous	
<b>Cost (1000 \$ / yr)</b>		<b>884.2</b>		<b>641.5</b>
<b>Utility</b>				
HP boiler flowrate (kg/s)	Yes	17.66	Yes	18.20
MP boiler flowrate (kg/s)	No		No	
Power demand external (kW)	HP → LP	7500	Extraction	7500
Reverse osmosis power demand (kW)	MP → LP	62.0	MP → LP	63.89
<b>HEN Utility (kW)</b>				
Cooling		1463.8		751.1
HP steam		3820.2		5727.2
MP steam		13628.2		21065.7
LP steam		4743.4		19110.2
F <sub>cp,H1</sub> (kW/K)		48		32
F <sub>cp,C2</sub> (kW/K)		144		216
<b>WN flowrate (kg/s)</b>				
Freshwater		7.26		6.47
Sand filter		7.2		6.4
Reverse osmosis		5.6		5.8
Scrubber		2.4		1.2

# Conclusion



- » Developed LP formulations for targeting minimum freshwater consumption for a set of water-using process units under a specific condition
- » Extended the water targeting formulation to nonisothermal water network
- » **Targeting method can be used to improve objective function and computational effort under the simultaneous approach for flowsheet optimization**
- » **The interaction among power use, heat use, and water use can be exploited to achieve better flowsheet design**

**Thank you!**

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